

acm International Collegiate Programming Contest

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Hilbert Sort

Sorting numerical data not only makes it easy to search for a particular item, but also makes better use of a CPU's cache: any segment of data that's contiguous in memory will describe a set of items that are similar in some sense. Things get more complicated if our data represents points on a 2D grid. If points (x,y) are sorted by x, breaking ties by y, then adjacent points will have similar x coordinates but not necessarily similar y, potentially making them far apart. To better preserve distances, we can sort the data along a space-filling curve.

The Hilbert curve starts at the origin (0,0), finishes at (s,0), in the process traversing every point in axis-aligned square with corners at (0,0) and (s,s). It has the following recursive construction: split the square into four quadrants meeting at (s/2, s/2). Number them 1 to 4, starting at the lower left and moving clockwise. Recursively fill each of them with a suitably rotated and scaled copy of the full Hilbert curve.

Start with a single point at (*s*/2,*s*/2). Then, repeat these steps:

- Scale and copy the current construction into each of the 4 quadrants.
- Rotate quadrant 1 by -90 degrees and flip it vertically, so that the start of the curve is closest to the lower left corner (**0**,**0**).
- Rotate quadrant 4 by 90 degrees and flip it vertically, so that the end of the curve is closest to the lower right corner (*s*,**0**).
- Now, connect the end of the curve in quadrant 1 to the start of the curve in quadrant 2, connect the end of quadrant 2 to the start of quadrant 3, and the end of quadrant 3 to the start of quadrant 4.

Here are the first two iterations:



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The Hilbert Curve is built by repeating this construction infinitely many times. The following diagram shows the first six steps of building the Hilbert Curve:



Given some places of interest inside of a square region, sort them according to when the Hilbert curve visits them, starting from (0,0). Without going into gory detail about Fractal theory, note that making **s** odd guarantees that all integer points are visited just once, so their visitation order in relation to each other is unambiguous.

Input

Each input will consist of a single test case. Note that your program may be run multiple times on different inputs. The first line of input contains two space-separated integers n and s ($1 \le n \le 100,000, 1 \le s < 10^9, s$ is odd). The next n lines describe locations of interest by space-separated integers x and y ($0 \le x, y \le s$). No two locations will share the same position.

Output

Output the n ordered pairs, one per line, with x and y separated by a space, Hilbertsorted according to their positions.







Sample Input	Sample Output
14 25	5 5
5 5	10 5
5 10	10 10
5 20	5 10
10 5	5 20
10 10	10 20
10 15	10 15
10 20	15 15
15 5	15 20
15 10	20 20
15 15	20 10
15 20	15 10
20 5	15 5
20 10	20 5
20 20	