# ACM International Collegiate Programming Contest 2014 East Central Regional Contest <br> Grand Valley State University <br> University of Cincinnati <br> University of Windsor <br> Youngstown State University November 8, 2014 

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## Rules:

1. There are nine problems to be completed in five hours.
2. All questions require you to read the test data from standard input and write results to standard output. You cannot use files for input or output. Additional input and output specifications can be found in the General Information Sheet.
3. When displaying results, follow the format in the Sample Output for each problem. Unless otherwise stated, all whitespace in the Sample Output consists of exactly one blank character.
4. The allowed programming languages are C, C++ and Java.
5. All programs will be re-compiled prior to testing with the judges' data.
6. Non-standard libraries cannot be used in your solutions. The Standard Template Library (STL) and C++ string libraries are allowed. The standard Java API is available, except for those packages that are deemed dangerous by contestant officials (e.g., that might generate a security violation).
7. The input to all problems will consist of multiple test cases.
8. Programming style is not considered in this contest. You are free to code in whatever style you prefer. Documentation is not required.
9. All communication with the judges will be handled by the $\mathrm{PC}^{2}$ environment.
10. Judges' decisions are to be considered final. No cheating will be tolerated.

## Problem A: $\quad$ Con $+\frac{\text { tin }}{\text { ued }+\frac{\text { Frac }}{\text { tions }}}$

The (simple) continued fraction representation of a real number $r$ is an expression obtained by an iterative process of representing $r$ as a sum of its integer part and the reciprocal of another number, then writing this other number as the sum of its integer part and another reciprocal, and so on. In other words, a continued fraction representation of $r$ is of the form

$$
r=a_{0}+\frac{1}{a_{1}+\frac{1}{a_{2}+\frac{1}{a_{3}+\ldots}}}
$$

where $a_{0}, a_{1}, a_{2}, \ldots$ are integers and $a_{1}, a_{2}, \ldots>0$. We call the $a_{i}$-values partial quotients. For example, in the continued fraction representation of 5.4 the partial quotients are $a_{0}=5, a_{1}=2$, and $a_{2}=2$. This representation of a real number has several applications in theory and practice.

While irrational numbers like $\sqrt{2}$ require an infinite set of partial quotients, any rational number can be written as a continued fraction with a unique, finite set of partial quotients (where the last partial quotient is never 1 in order to preserve uniqueness). Given two rational numbers in continued fraction representation, your task is to perform the four elementary arithmetic operations on these numbers and display the result in continued fraction representation.

## Input

Time Limit: 3 secs, No. of Test Cases: 500, Input File Size 13.1K
Each test case consists of three lines. The first line contains two integers $n_{1}$ and $n_{2}, 1 \leq n_{i} \leq 9$ specifying the number of partial quotients of two rational numbers $r_{1}$ and $r_{2}$. The second line contains the partial quotients of $r_{1}$ and the third line contains the partial quotients of $r_{2}$. The partial quotients satisfy $\left|a_{0}\right| \leq 10$ and $0<a_{i} \leq 10$, the last partial quotient will never be 1 , and $r_{2}$ is non-zero. A line containing two 0 's will terminate input.

## Output

For each test case, display the case number followed by the continued fraction representation of $r_{1}+r_{2}$, $r_{1}-r_{2}, r_{1} \times r_{2}$, and $r_{1} / r_{2}$ in order, each on a separate line. Use 64 -bit integers for all of your calculations (long long in C++ and long in Java).

## Sample Input

43
5112
522
00

## Sample Output

```
Case 1:
```

11
05
3046
127

## Problem B: A Cure for the Common Code

You've been tasked with relaying coded messages to your fellow resistance fighters. Each coded message is a sequence of lower-case letters that you furtively scrawl on monuments in the dead of night.

Since you're writing these messages by hand, the longer the message, the greater the likelihood of being caught by the evil empire while writing. Because of this you decide it would be worthwhile to come up with a simple encoding that might allow for shorter messages. After thinking about it for a while, you decide to use integers and parentheses to indicate repetition of substrings when doing so shortens the number of characters you need to write. For example, the 10 character string

> abcbcbcbca
could be more briefly written as the 7 character string

$$
\mathrm{a} 4(\mathrm{bc}) \mathrm{a}
$$

If a single letter is being repeated, parentheses are not needed. Also, repetitions may themselves be repeated, so you can write the 20 character string

abbbcdcdcdabbbcdcdcd

as the 11 character string

$$
2(\mathrm{a} 3 \mathrm{~b} 3(\mathrm{~cd}))
$$

and so forth.
Input Time Limit: 5 secs, No. of Test Cases: 39, Input File Size 2.95K
Each test case consists of a single line containing a string of lower-case letters of length $\leq 500$. A line containing a single 0 will terminate the input.

## Output

For each test case, output the number of characters needed for a minimal encoding of the string.

## Sample Input

abcbcbcbca
abbbcdcdcdabbbcdcdcd
0

## Sample Output

Case 1: 7
Case 2: 11

## Problem C: Domiyahtzee!

Yahtzee is a well known dice game in which players get points for various combinations of five dice rolls. Some of the combinations and their payoffs are shown Table 1 (note: the payoffs for the first two are slightly different than in the official rules of Yahtzee):

| Combination | Description | Points |
| :--- | :--- | :--- |
| 3-of-a-Kind | 3 dice showing same face | Sum of the three dice |
| 4-of-a-Kind | 4 dice showing same face | Sum of the four dice |
| Full House | 3-of-a-Kind and a pair | 25 |
| Small Straight | 4 consecutive values on any 4 dice | 30 |
| Large Straight | 5 consecutive values | 40 |
| Yahtzee | 5 dice showing same face | first Yahtzee - 50 <br> subsequent Yahtzees - 100 each |

Table 1

Domiyahtzee! is a well known version of Yahtzee which we just invented. It uses a standard set of 21 dominoes containing all possible combinations of the numbers 1 through 6 - ( 1,1 ), ( 1,2 ), $\ldots,(1,6),(2,2)$, $(2,3), \ldots,(6,6)$. The game is played as follows: you are given a $5 \times 5$ grid which is filled with 12 of the 21 dominoes along with a value between 1 and 6 placed in a random square. An example grid is shown below - the " 4 " in the fourth row and column is the lone "singleton" value:


Figure 1

You score points in Domiyahtzee! for each combination in Table 1 found in any row, column or long diagonal. The grid above would score for the Full House in row 1, the Small Straight in row 4, the 3 -of-a-Kind in column 1, the Small Straight in column 3, the 4 -of-a-Kind in column 5 and the Full House in the first long diagonal for a total score of $25+30+9+30+16+25=135$. However, you can attempt to improve your score by replacing any one domino on the grid with any of the remaining 9 unused dominoes. For example, if you were to replace the $(5,5)$ in the first row with the unused $(6,6)$ domino, the grid would now score 50 (for the Yahtzee in row 1) $+30+9+18$ (for the new 3 -of-a-Kind in column 2) +40 (for the new Large Straight in column 3) $+16+25=188$. The object of the game, of course, is to find the replacement which maximizes your score. In the above example, replacing the $(5,6)$ in row 5 with a $(3,2)$ leads to the highest scoring grid.

## Input Time Limit: 3 secs, No. of Test Cases: 51, Input File Size 3.88 K

The input file starts with an integer $n$ indicating the number of test cases in the file. Each test case consists of 13 domino specifications of the form $\mathrm{H} n_{1} n_{2}$, V $n_{1} n_{2}$, or $\mathrm{S} n_{1}$, indicating either a horizontal or vertical domino, or a singleton value (there is exactly 1 singleton in each test case). These specifications may be over multiple lines. As you read in each domino specification you place it in the first available location going row-wise left-to-right, top-to-bottom.

## Output

For each test case, output the maximum obtainable score for the given grid of dominoes involving at most one domino replacement.

## Sample Input

1
V 63 H 55 V 62 V 64 V 61
V 34 V 33 H 14 H 52 S 4 V 44
H 56 H 51

## Sample Output

Case 1: 218

## Freetime Challenge!

What's the highest scoring Domiyahtzee grid that you can make? Our highest scoring grid is worth 498 points.

## Problem D: Generalized Roman Numerals

The ancient Romans developed a terrible numbering system in which I, V, X, L and C stood for 1, $5,10,50$ and 100 , respectively. So XXXVII represents $37(10+10+10+5+1+1)$. They typically wrote the numerals in non-increasing order. However, when a single Roman numeral is written before one that is larger, we subtract the smaller from the larger. So we can write IV and IX to represent 4 and 9 (subtracting 1), or XL and XC to represent 40 and 90 (subtracting 10). To represent 94 , we would write XCIV.

VIC is generally not considered a traditional Roman numeral, but we can interpret this as another representation of 94 : VI is 6 , so VIC is $100-6$. In general, if we have two expressions $a$ and $b$ representing values $v(a)$ and $v(b)$, then we say that $v(a b)$ is $v(a)+v(b)$ if $v(a) \geq v(b)$, and $v(b)-v(a)$ otherwise.
Unfortunately, this generalization introduces some ambiguity, since different orders of evaluation may result in different values. For example, consider IVX: IV is 4 and X is 10 , so by that reasoning IVX is 6. However, I is 1 and VX is 5 , so this suggests that IVX is actually 4. To remedy this ambiguity, we allow the addition of parentheses. The question arises: for a given string of Roman numeral characters, how many different values can be obtained using different placements of parentheses?

## Input <br> Time Limit: 3 secs, No. of Test Cases: 33, Input File Size 0.678K

Each test case consists of a single string containing only the characters I, V, X, L and C. The length of this string will be $\leq 50$. A line containing of a single 0 will terminate input.

## Output

For each test case, output all possible distinct values that can be represented by the string via the addition of parentheses. Display these values in increasing order.

## Sample Input

IVX
XIXIX
0

## Sample Output

Case 1: 46
Case 2: 810283032

## Problem E: Inspectors

Yuri is a rich business owner. His company has factories in many cities across Russia, all of which need regular, monthly inspections. Now Yuri not only has a large portfolio, but a large family as well and he would like to see some of his children start to learn how the business is run. He figures the best way to do this is to have them perform the factory inspections, but he has two concerns. First, he wants each child to be assigned at least two different factories - that way they will be able to compare different management styles at the factories and get a better idea of what works and what doesn't work. This of course requires them to travel between the factories, which brings up Yuri's second problem: while he won't be paying his children anything (their weekly allowance is more than adequate), he's worried about the total of all the travel costs, and would like it to be as small as possible. Each child is expected to inspect each of their assigned factories once a month, always ending back at the factory they started at, so to minimize cost he figures he need only assign the factories to minimize the total distance of these factory tours. The more he thinks about this, the more important saving money becomes. He's willing to use as few as only one of his children if that's the cheapest way to inspect all the factories. For example, if Yuri had four factories placed as in the figure on the left below, he could employ just one child, who could visit each factory for a monthly distance of 40 (assume here that the unlisted distances between factories are all $>10$ ). However, if his factories were located as shown on the right, he would need to employ two children to obtain the monthly minimal distance of 40 (note: he could use two children to achieve the minimal distance in the first figure as well).


Since the number of factories changes over time, Yuri would like a program to determine the minimum distance he can expect for any layout of factories.

## Input Time Limit: 3 secs, No. of Test Cases: 101, Input File Size 624K

The input file begins with a line containing a single integer $m$ indicating the number of test cases. Each test case starts with an integer $n$ indicating the number of factories, where $2 \leq n \leq 100$. The next $n-1$ lines contain the positive integer distances between the factories: line 1 contains $n-1$ values specifying the distances between factory 1 and factories $2,3,4, \ldots, n$; line 2 contains $n-2$ values specifying the distances between factory 2 and factories $3,4, \ldots, n$; and so on. The maximum distance between any two factories is 1000 .

## Output

For each test case display the minimum factory tour distance. You should always assume that Yuri has at least $n / 2$ kids for each set of $n$ factories.

## Sample Input

2
4
$10 \quad 2010$
1020
10
4
152010
1020
15

## Sample Output

Case 1: 40
Case 2: 40

## Problem F: Path of Least Persistence

Bob Roberts owns a company that makes novelty games for parties. One of his favorites is a puzzle labyrinth, where players must navigate a path through a rectangular grid based on puzzles they must solve at each grid location. The solution to each puzzle indicates which grid square to go to next, and this continues until the player reaches the destination square. Bob has software to lay out the intended path, but there was a glitch in the algorithm and the resulting grids often have either very long paths or paths that don't lead to the destination. For example, consider the 3 x 3 grid shown on the left in Figure 1.


Figure 1
The solution to each puzzle is shown in each grid square, which gives the number of squares to move and the direction to move (either North, South, East or West). In this grid the path from the start square (always the upper left) to the destination square (always the lower right) has six segments, which is very unsatisfying to many customers (who aren't persistent enough to solve so many puzzles). Bob noticed this when setting up the grid, and because he didn't have much time, he looked to see if there was one grid square solution he could change to make the path shorter. After a quick look, he changed the puzzle in the upper left square so that its solution changed from 2 E to 1 E (the middle figure) which led to a path of length 3 - not ideal, but better than the original path. After the party was over, Bob realized that there was an even better solution, shown in the right figure, that led to a path of length 2 (note that by path length we mean the number of puzzles solved while on the path)
Changing a solution to a puzzle is somewhat complicated and time consuming, so Bob only wants to change at most one puzzle when setting up a grid. He has come to you to help solve the following problem: given a grid layout, which is the one square direction to change to minimize the path from the start to the destination. Bob realizes that sometimes there is no answer (since it might take two or more changes to actually get a path) and sometimes there is no need to change any square, since any change would result in a path no shorter than the one that already exists. He is confident that you can handle all these cases.

## Input

Time Limit: 3 secs, No. of Test Cases: 76, Input File Size 1157K
The first line of each case contains two positive integers $n m$ indicating the number of rows and columns in the grid, where $n, m \leq 100$. Following that are $n m-1$ direction specifications for the grid, given row-wise left to right starting at the topmost row. These are in the form $r \mathrm{D}$, where $r$ is the number of grid squares to move and $D$ is the direction to move, either ' $N$ ' (up), ' $S$ ' (south), ' $E$ ' (right), or ' $W$ ' (you figure it out). Each grid will contain at least 2 grid squares. A line containing two 0 's will terminate input.

## Output

For each test case, output the case number followed by one of three possible answers. If there is no way to change one square to get a path to the destination, output impossible. If the existing path in the grid cannot be made shorter, output none $l$, where $l=$ length of the existing path. Otherwise, output the row and column of the square to change (where the top row is row 0 and the leftmost column is column 0 ) followed by the new direction for that square, followed by the length of the new, shortest path. If there are two or more changes that could be used, display the one that has the lowest row number. If there are two or more with the lowest row number, display the one with the lowest column number. Finally, if there is still a tie use the change that comes first in the following ordering: $1 \mathrm{E}<1 \mathrm{~N}$ $<1 \mathrm{~S}<1 \mathrm{~W}<2 \mathrm{E}<\ldots$ etc.

## Sample Input

```
3 3
2E 2S 1S 1S 1N 1W 2N 1E
24
1E 1W 1W 1W 1W 1W 1W
14
3E 1E 1E
O
```


## Sample Output

```
Case 1: 0 2 2S 2
Case 2: impossible
Case 3: none 1
```


## Problem G: Speed Skills

Anna has just gotten a new car and is dying to take it out on the highway. To minimize her chance of getting a speeding ticket she wants to make sure she is not going that much faster than anyone else on the highway. However, she doesn't want to go too slow, regardless of the speed of the other drivers. She has hit on the following strategy. Every time she passes a car, she will reduce her speed to the average of her old speed and the other car's speed; when she is passed by someone, she increases her speed likewise. To carry out this strategy, she has built a little gizmo which checks for passing or passed cars 4 times each second. It then adjusts her car's speed to the average of her current speed and those of all the cars either being passed or passing her, rounding the average down to the nearest integer. For example, if at a particular quarter second Anna is going 60 , is being passed by a car going 65 and is also passing another car going 59 , her car changes its speed to $\lfloor(60+65+59) / 3\rfloor=61$. For the purposes of this problem, Anna's car is considered passing or being passed if the front of the other car is anywhere between the back and front of Anna's car, inclusive. All cars will be considered to have the same length and all cars (except Anna's) travel at a constant speed. Also, assume that Anna's car changes speed instantaneously.

## Input

Time Limit: 3 secs, No. of Test Cases: 50, Input File Size 32.6K
The first line of each test case contains four non-negative integers $l s d n$, where $l$ is Anna's current location on the highway (in car lengths), $s$ is her current speed (in car lengths per second), $d$ is the location of a destination point on the highway (where $l<d \leq 100000000$ ), and $n$ is the number of other vehicles on the road (all going in Anna's direction). The maximum value of $n$ is 100 . The next $n$ lines contains $n$ pairs of integers $l_{i} s_{i}, 1 \leq i \leq n$, indicating the location and speed of each of the other $n$ vehicles. All locations refer to the front of the car in question. All input refers to location and times at time $t=0$, which is also the time Anna's gizmo takes its first reading. A line containing four 0 's will terminate input.

## Output

For each test case output a single line containing the time Anna reaches the destination point (in seconds) and her current speed at that time (in car lengths per second), using the format shown below. The destination point is considered reached the moment the front of Anna's car reaches it. If her destination arrival time is on a quarter second and she is being passsed or is passing someone at that same instant, output her new averaged speed. Round all output to the nearest ten-thousandth.

## Sample Input

3002010002
20030
240
3002010002
20030
10040
0000

## Sample Output

Case 1: Anna reaches her destination at time 27.0469 at a speed of 32
Case 2: Anna reaches her destination at time 26.6667 at a speed of 30

## Problem H: Time Warp

Tim Ang is a bit of a nerd. Check that - he's a HUGE nerd. When you ask him the time, he might say something like " 20 after 8 ", which seems normal, but other times he'll say things like " 90 after 8 " or "126 til 4", which gives you pause. When you ask him about this, Tim say that " 20 after 8 " means the first time after 8 that the hour and minute hands of the clock make an angle of 20 degrees; " 126 til 4 " means the closest time before 4 that the hands make an angle of 126 degrees. As Tim walks away snickering, you resolve that you will write a program that will automatically convert Tim's times to our more normal, non-nerdy times. That'll show the little geek!

Input
Time Limit: 3 secs, No. of Test Cases: 8640, Input File Size 94.6K
The input file starts with an integer $n$ indicating the number of test cases. Each test case consists of a single line of the form $a$ after $b$ or $a$ til $b$, where $a$ and $b$ are integers satisfying $0 \leq a<360$, and $1 \leq b \leq 12$. All angles are measured starting at the hour hand and moving clockwise until reaching the minute hand (so, for example, at 9 o'clock the hands make an angle of 90 degrees and at 3 o'clock they make an angle of 270).

## Output

For each test case, output the time in the format $\mathrm{h}: \mathrm{m}: \mathrm{s}$, where $\mathrm{h}, \mathrm{m}$ and s are the hour, minutes and seconds closest to the given angle and hour. Always use two digits to represent the number of minutes and seconds.

## Sample Input

4
20 after 8
126 til 4
180 til 1
0 after 12

## Sample Output

Case 1: 8:47:16
Case 2: 3:39:16
Case 3: 12:32:44
Case 4: 1:05:27

## Problem I: Watch, Man!

Lou Va is the curator of a world-renowned art museum. While he has hundreds of pieces of artwork on display, there are certain ones that are extremely valuable and need extra levels of security. Lou has set up a collection of security locations throughout the museum and plans to place security guards there to keep an eye on the valuable art.
After careful analysis of the art pieces and the security guards' resumes, Lou has assigned different levels to each art piece and each guard. A level $n$ art piece is one which must be in view of at least $n$ security guards. A level $m$ security guard is one who has enough experience to keep an eye on up to $m$ pieces of art. Lou wants to place the guards so that each piece of art can be watched by the appropriate number of guards.

One more complication: this is a modern-art musuem, and its layout is non-conventional. Walls of all the rooms are either straight line segments or arcs of circles. The first two layouts in Figure 1 show one such room, with different placements of guards and art pieces (with their respective level values shown). In addition, there may be one or more interior sets of walls that can block the guards' views, as shown in the third layout below. Any set of interior walls forms a simple closed loop, and if there is more than one such set of interior walls, none will intersect or nest within each other.


Figure 1
As the second and third examples show, sometimes the placements of the guards is not sufficient to watch all of the art pieces. Lou needs to know this, as he will then change either the placements of the guards or the art pieces. He has come to you for some help.

## Input Time Limit: 3 secs, No. of Test Cases: 48, Input File Size 23.7 K

The first line of each test case contains three integers $n a g$ indicating the number of wall sets, art pieces and guards, respectively, where $1 \leq n$ and $0 \leq a, g \leq 100$. Following this are descriptions of each of the $n$ wall sets, where the first set is the set of outer walls. Each description starts with an integer $m$ indicating the number of walls in the wall set. This is followed by $m$ sets of integer coordinates $x_{i}$ $y_{i}$ each followed by either an ' $s$ ' or a ' $c$ '. An ' $s$ ' indicates that point $\left(x_{i}, y_{i}\right)$ should be connected by a straight-line wall to the next point, and a ' $c$ ' indicates it should be connected with a circular arc. Following a ' $c$ ' are two integers giving the $d x$ and $d y$ values of the tangent line of the circle at the point $\left(x_{i}, y_{i}\right)$. Two examples of this are shown in Figure 2.


Figure 2
The total number of walls for all the rooms in any test case will be $\leq 125$. Following the wall specifications are $a$ integer coordinates giving the location of the art pieces, each followed by a positive level number. Next are $g$ integer coordinates giving the location of the guards, each followed by a positive level number. No wall corner will lie on a line segment connecting an art piece and a guard, and no line between an art piece and a guard will ever be tangent to a curved wall. All coordinates are in the range -150000 to 150000 . A line containing three 0 's will terminate input.

## Output

For each test case, output the case number and either Yes or No indicating whether or not the guards in their current locations can watch the art pieces at the appropriate levels.

## Sample Input (shown across multiple columns)

| 132 | 132 | 232 |
| :---: | :---: | :---: |
| 5 | 5 | 5 |
| 00 s | 00 s | 00 s |
| 020 c 01 | 020 c 01 | 020 c 01 |
| 2020 s | 2020 s | 2020 s |
| 4020 s | 4020 s | 4020 s |
| 400 s | 400 s | 400 s |
| 2181 | 2181 | 2 |
| 15182 | 18242 | 2319 c 10 |
| 3822 | 3822 | 1511 s |
| 223 | 223 | 2181 |
| 38182 | 38182 | 15182 |
|  |  | 3822 |
|  |  | 223 |
| Sample Output |  | 38182 |
| Case 1: Yes |  | 000 |
| Case 2: No |  |  |
| Case 3: No |  |  |

